

Transverse Structure of Nucleon Parton Distributions

Dru B. Renner

University of Maryland

November 19, 2003

Generalized parton distributions determine the angular momentum decomposition of the nucleon and the transverse distribution of partons in the nucleon. Additionally, in particular limits they reduce to form factors and ordinary parton distributions. I will review generalized parton distributions and present our full QCD lattice calculations of the quark helicity and orbital angular momentum in the nucleon, the asymptotic scaling ratio F_2/F_1 , and the transverse distribution of quarks in the nucleon.

Transverse Structure of Nucleon Parton Distributions

Dru B. Renner

University of Maryland

November 19, 2003

Collaborators

R. Brower

R. Edwards

G. Fleming

Ph. Hagler

U. Heller

Th. Lippert

J. Negele

A. Pockinsky

D. Richards

K. Schilling

W. Schroers

http://drubryantrenner.org/talks/umd_11-19-03.pdf

Outline

- I. Continuum Physics Review
- II. Transverse Nucleon Structure
- III. Lattice Calculation
- IV. Our Results

Continuum Physics Review

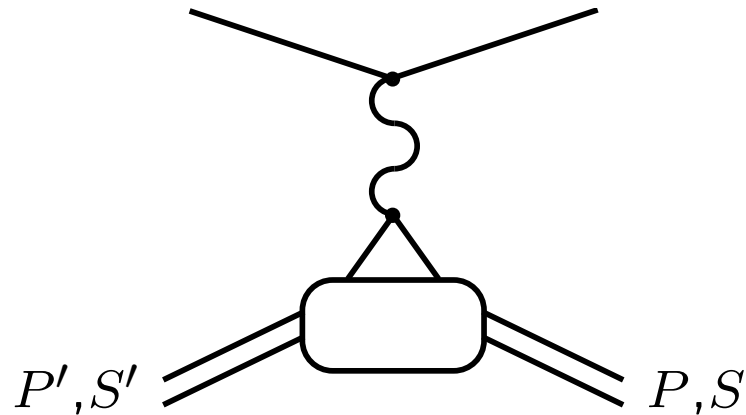
I. Form Factors

II. Parton Distributions

III. Generalized Parton Distributions

Form Factors

- lepton-nucleon scattering, $lN \rightarrow lN$, elastic



$$\Delta = P' - P$$

$$t = \Delta^2$$

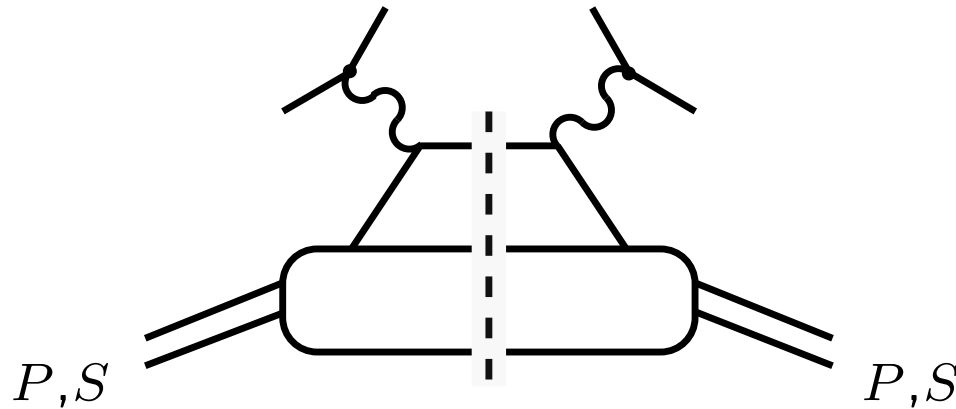
- off-forward matrix element of the electromagnetic current

$$\langle P', S' | J^\mu | P, S \rangle = \bar{U}(P', S') \left(\gamma^\mu F_1(t) + \frac{i\sigma^{\mu\nu} \Delta_\nu}{2m} F_2(t) \right) U(P, S)$$

- interpretation as Fourier transform of charge and current densities *in certain cases*
- magnetic moment, charge & current radii

Parton Distributions

- deep inelastic scattering, $lN \rightarrow lX$, inclusive



$$P^+ = \frac{1}{2} (P^t + P^z)$$

$$y^- = \frac{1}{2} (y^t - y^z)$$

- forward matrix element of light-cone quark correlator

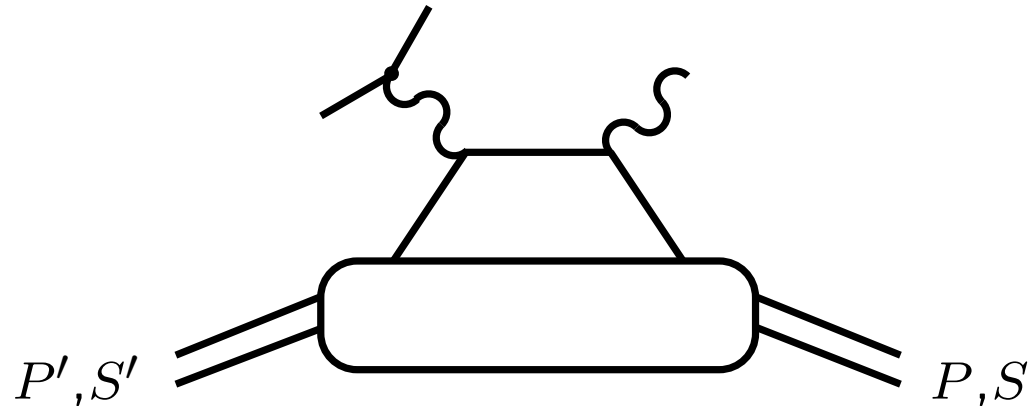
$$\mathcal{O}_q(x, \vec{b}_\perp) = \int \frac{dy^-}{4\pi} e^{ixP^+y^-} \bar{q} \left(-\frac{y^-}{2}, \vec{b}_\perp \right) \gamma^+ q \left(\frac{y^-}{2}, \vec{b}_\perp \right)$$

$$\langle P, S | \mathcal{O}_q(x, \vec{0}_\perp) | P, S \rangle = q(x)$$

- longitudinal momentum distribution in the *infinite momentum frame*
- momentum fraction & spin fraction

Generalized Parton Distributions

- deeply virtual Compton scattering, $lN \rightarrow lN\gamma$, exclusive



$$\bar{P} = \frac{1}{2} (P' + P)$$

$$\xi = -\frac{\Delta^+}{2\bar{P}^+}$$

- off-forward matrix element of light-cone quark correlator

$$\langle P', S' | \mathcal{O}_q(x, \vec{0}_\perp) | P, S \rangle =$$

$$\frac{1}{2\bar{P}^+} \bar{U}(P', S') \left(\gamma^+ H(x, \xi, t) + i \frac{\sigma^{+\nu} \Delta_\nu}{2M} E(x, \xi, t) \right) U(P, S)$$

Generalized Parton Distributions

- familiar limits: parton distributions & form factors

$$H_q(x, 0, 0) = q(x)$$

$$\sum_q e_q \int dx H_q(x, \xi, t) = F_1(t)$$

$$\sum_q e_q \int dx E_q(x, \xi, t) = F_2(t)$$

- quark angular momentum, [1]

$$J_q = \frac{1}{2} \int dx x (H_q(x, 0, 0) + E_q(x, 0, 0))$$

- transverse quark distribution in *infinite momentum frame* [2]

$$\int d^2b_\perp e^{i\vec{\Delta}_\perp \cdot \vec{b}_\perp} q(x, \vec{b}_\perp) = H_q(x, 0, -\vec{\Delta}_\perp^2)$$

[1] Ji hep-ph/9603249

[2] Burkardt hep-ph/0005108

Transverse Structure

- I. Charge Distribution: Non-Relativistic Limit
- II. Transverse Distribution: Infinite Momentum Frame

Charge Distribution: Non-Relativistic Limit

- wave packet

$$|\psi\rangle = \int \frac{d^3p}{(2\pi)^{3/2}} \frac{\psi(\vec{p})}{\sqrt{2E_{\vec{p}}}} |\vec{p}\rangle$$

- Fourier transform of charge distribution

$$\begin{aligned} \int d^3x e^{i\vec{q}\cdot\vec{x}} \langle\psi| J^0(\vec{x}) |\psi\rangle &= \\ &= \int d^3p \psi^*(\vec{k}) \psi(\vec{p}) \langle\vec{k}| J^0(0) |\vec{p}\rangle / \left(2\sqrt{E_{\vec{k}}E_{\vec{p}}}\right) \\ &= \int d^3p \psi^*(\vec{k}) \psi(\vec{p}) F(q^2) (E_{\vec{k}} + E_{\vec{p}}) / \left(2\sqrt{E_{\vec{k}}E_{\vec{p}}}\right) \end{aligned}$$

where $\vec{k} = \vec{p} + \vec{q}$ & $\langle\vec{k}| J^0(0) |\vec{p}\rangle = F(q^2) (E_{\vec{k}} + E_{\vec{p}})$

Charge Distribution: Non-Relativistic Limit

- non-relativistic limit $|\vec{q}| \ll M \quad E_{\vec{k}} \approx E_{\vec{p}} \quad q^2 \approx -\vec{q}^2$
- broad wave packet $\psi(\vec{k}) \approx \psi(\vec{p})$

$$\begin{aligned} & \int d^3x e^{i\vec{q}\cdot\vec{x}} \langle \psi | J^0(\vec{x}) | \psi \rangle \\ &= \int d^3p \psi^*(\vec{k}) \psi(\vec{p}) F(q^2) \left(\frac{E_{\vec{k}} + E_{\vec{p}}}{2\sqrt{E_{\vec{k}}E_{\vec{p}}}} \right) \\ &\approx \int d^3p \psi^*(\vec{p}) \psi(\vec{p}) F(-\vec{q}^2) \\ &\approx F(-\vec{q}^2) \end{aligned}$$

Charge Distribution: Non-Relativistic Limit

- separation of scales, $L_{FF/WP}$ is the form factor/wave packet length scale

$$L_{FF} \sim \frac{1}{|\vec{q}|} \gg L_{WP} \gg \frac{1}{M} \quad \Rightarrow \quad L_{FF} \gg \frac{1}{M}$$

- hydrogen atom

$$L_{FF} = \frac{1}{\alpha m_e} = 7 \cdot 10^4 \text{ fm} \gg \frac{1}{M_H} = \frac{1}{M_P} = 0.2 \text{ fm}$$

- proton

$$L_{FF} = 0.87 \text{ fm} \approx \frac{1}{M_P} = 0.2 \text{ fm}$$

Transverse Distribution: Infinite Momentum Frame

- wave packet

$$|\psi\rangle = \int \frac{d^2p_\perp}{(2\pi)} \frac{\psi(\vec{p}_\perp)}{\sqrt{2E_{\vec{p}}}} |\vec{p}_\perp, P_z\rangle \quad \vec{p} = (\vec{p}_\perp, P_z)$$

- Fourier transform of transverse quark distribution

$$\mathcal{O}_q(x, \vec{b}_\perp) = \int \frac{dy^-}{4\pi} e^{ixp^+y^-} \bar{q}(-y^-/2, \vec{b}_\perp) \gamma^+ q(y^-/2, \vec{b}_\perp)$$

$$\int d^2b_\perp e^{i\vec{\Delta}_\perp \cdot \vec{b}_\perp} \langle \psi | \mathcal{O}_q(x, \vec{b}_\perp) | \psi \rangle = \int d^2p_\perp \psi^*(\vec{k}_\perp) \psi(\vec{p}_\perp) H_q(x, 0, \Delta^2) (2\sqrt{E_{\vec{k}}}\sqrt{E_{\vec{p}}})$$

$$\vec{k}_\perp = \vec{p}_\perp + \vec{q}_\perp \quad k_z = p_z = P_z \quad \langle \vec{k} | \mathcal{O}_q(x, \vec{0}_\perp) | \vec{p} \rangle = H_q(x, 0, \Delta^2)$$

Transverse Distribution: Infinite Momentum Frame

- infinite momentum limit $|\vec{q}_\perp| \ll P_z$ $E_{\vec{k}} \approx E_{\vec{p}}$ $\Delta^2 \approx -\vec{\Delta}_\perp^2$
- broad wave packet $\psi(\vec{k}_\perp) \approx \psi(\vec{p}_\perp)$

$$\begin{aligned} & \int d^2 b_\perp e^{i\vec{\Delta}_\perp \cdot \vec{b}_\perp} \langle \psi | \mathcal{O}_q(x, \vec{b}_\perp) | \psi \rangle \\ &= \int d^2 p_\perp \psi^*(\vec{k}_\perp) \psi(\vec{p}_\perp) H_q(x, 0, \Delta^2) / (2\sqrt{E_{\vec{k}}} \sqrt{E_{\vec{p}}}) \\ &\approx \int d^2_\perp p \psi^*(\vec{k}_\perp) \psi(\vec{p}_\perp) H_q(x, 0, -\vec{\Delta}_\perp^2) / 2P_z \\ &\approx H_q(x, 0, -\vec{\Delta}_\perp^2) / 2P_z \end{aligned}$$

Transverse Distribution: Infinite Momentum Frame

- separation of scales, L_{TD}/L_{WP} is the transverse distribution/wave packet length scale

$$L_{TD} \sim \frac{1}{|\vec{q}|} \gg L_{WP} \gg \frac{1}{\sqrt{M^2 + P_z^2}} \quad \Rightarrow \quad L_{TD} \gg \frac{1}{\sqrt{M^2 + P_z^2}} \rightarrow 0$$

- transverse quark distribution

$$\int d^2b_{\perp} e^{i\vec{\Delta}_{\perp} \cdot \vec{b}_{\perp}} q(x, \vec{b}_{\perp}) = H_q(x, 0, -\vec{\Delta}_{\perp}^2)$$

Lattice Calculation

- I. Moments of Generalized Parton Distributions
- II. Generalized Form Factors
- III. Matrix Elements from Lattice QCD

Moments of Generalized Parton Distributions

- generalized parton distributions

$$\langle P', S' | \mathcal{O}_q(x) | P, S \rangle = \frac{1}{2\bar{P}^+} \bar{U}(P', S') \left(\gamma^+ H_q(x, \xi, t) + i \frac{\sigma^{+\nu} \Delta_\nu}{2M} E_q(x, \xi, t) \right) U(P, S)$$

$$\mathcal{O}_q(x, \vec{b}_\perp) = \int \frac{dy^-}{4\pi} e^{ixP^+y^-} \bar{q} \left(-\frac{y^-}{2}, \vec{b}_\perp \right) \gamma^+ q \left(\frac{y^-}{2}, \vec{b}_\perp \right)$$

- light-cone expansion & tower of twist 2 operators

$$\mathcal{O}_q^{\mu_1 \mu_2 \dots \mu_n} = \bar{q} \gamma^{\{\mu_1} i D^{\mu_2} \dots i D^{\mu_n\}} q$$

- moments of generalized parton distributions

$$\langle P' | \mathcal{O}^{\mu_1, \mu_2, \dots, \mu_n} | P \rangle \sim \int dx x^{n-1} H_q(x, \xi, t) \quad \& \quad \int dx x^{n-1} E_q(x, \xi, t)$$

Generalized Form Factors

- $n + 1$ generalized form factors

$$\langle P' | \mathcal{O}_q^{\mu_1 \mu_2 \dots \mu_n} | P \rangle \sim A_{ni}^q(t), B_{ni}^q(t), C_n^q(t)$$

- moments of parton distributions

$$\langle x^{n-1} \rangle_q = A_{n0}^q(0)$$

- form factors

$$F_1(t) = \sum_q e_q A_{10}^q(t) \quad F_2(t) = \sum_q e_q B_{10}^q(t)$$

- quark angular momentum

$$J_q = \frac{1}{2} (A_{20}^q(0) + B_{20}^q(0))$$

Generalized Form Factors

- moments of generalized parton distributions

$$\int_{-1}^1 dx x^{n-1} H_q(x, \xi, t) = \sum_{i=0}^{[(n-1)/2]} A_{n,2i}^q(t) (-2\xi)^{2i} + \text{mod}(n+1, 2) C_n^q(t) (-2\xi)^n$$

$$\int_{-1}^1 dx x^{n-1} E_q(x, \xi, t) = \sum_{i=0}^{[(n-1)/2]} B_{n,2i}^q(t) (-2\xi)^{2i} - \text{mod}(n+1, 2) C_n^q(t) (-2\xi)^n$$

- transverse momentum transfer, $\xi \rightarrow 0$

$$\int_{-1}^1 dx x^{n-1} H_q(x, 0, t) = A_{n0}^q(t)$$

$$\int_{-1}^1 dx x^{n-1} E_q(x, 0, t) = B_{n0}^q(t)$$

Lattice Correlation Functions

- correlation function of $2N$ fermion fields $(\psi, \bar{\psi})$ and M gauge links ($U = e^{iagA}$)

$$\begin{aligned} \langle \psi_1 \cdots \psi_N \bar{\psi}_1 \cdots \bar{\psi}_N U_1 \cdots U_M \rangle &= \\ &= \int DU \int D\psi D\bar{\psi} e^{-S_G[U]} e^{-\bar{\psi} M[U] \psi} \psi_1 \cdots \psi_N \bar{\psi}_1 \cdots \bar{\psi}_N U_1 \cdots U_M \\ &= \int DU e^{-S_G[U]} \det^{N_f}(M[U]) U_1 \cdots U_M \sum_{\pi} (-1)^{\pi} M[U]_{1\pi_1}^{-1} \cdots M[U]_{N\pi_N}^{-1} \end{aligned}$$

- numerical integration

$$\int DU e^{-S_G[U]} \det^{N_f}(M[U]) F[U] = \lim_{N \rightarrow \infty} \frac{1}{N} \sum_{i=1}^N F[U^i]$$

Matrix Elements from Lattice Correlation Functions

- nucleon interpolating field with gauge invariant smearing

$$J^\alpha = U_a^\alpha (U_b^T C \gamma^5 D_c) \epsilon_{abc}$$

- lattice ratios: fixed source (src), momentum projection at operator (op), sink (snk)

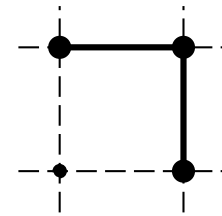
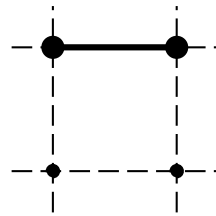
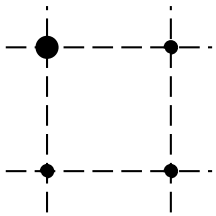
$$\langle p', s' | \mathcal{O} | p, s \rangle \sim \frac{\langle J(x_{\text{snk}}) \mathcal{O}(x_{\text{op}}) \bar{J}(x_{\text{src}}) \rangle}{\langle J(x_{\text{snk}}) \bar{J}(x_{\text{src}}) \rangle}$$

- quantum mechanical matrix elements are given by appropriate ratios of lattice correlation functions

Building Blocks

- two quark operators can be written in terms of a basic set of building blocks

$$\bar{q}(x) \Gamma_i q(x) \quad \bar{q}(x + \hat{\mu}) \Gamma_i U_\mu^\dagger(x) q(x) \quad \bar{q}(x + \hat{\nu} + \hat{\mu}) \Gamma_i U_\nu^\dagger(x + \hat{\mu}) U_\mu^\dagger(x) q(x)$$



- Γ_i ($i = 1, \dots, 16$) denote a complete basis of 4×4 Dirac spin matrices
- calculate upto 3 gauge link insertions: $U_{\mu_n}^\dagger(x + \hat{\mu}_{n-1} + \dots + \hat{\mu}_1) \dots U_{\mu_1}^\dagger(x)$
- calculate a broad range of momentum transfers \vec{q}

Overdetermined Set of Lattice Observables

- i labels all combinations of operator indices (μ_1, \dots, μ_n) and momenta P', P

$$\mathcal{O}_i^{\overline{\text{MS}}} = \langle P' | \mathcal{O}^{\mu_1, \dots, \mu_n} | P \rangle$$

- expand $\mathcal{O}_i^{\overline{\text{MS}}}$ in terms of generalized form factors

$$\mathcal{O}_i^{\overline{\text{MS}}} = \sum_{\alpha=1}^{n+1} A_{i\alpha} F_\alpha(t)$$

- match $\mathcal{O}_i^{\overline{\text{MS}}}$ to $\mathcal{O}_i^{\text{lat}}$ with one loop matching coefficients Z_{ij}

$$\mathcal{O}_i^{\overline{\text{MS}}} = \sum_j Z_{ij} \mathcal{O}_j^{\text{lat}}$$

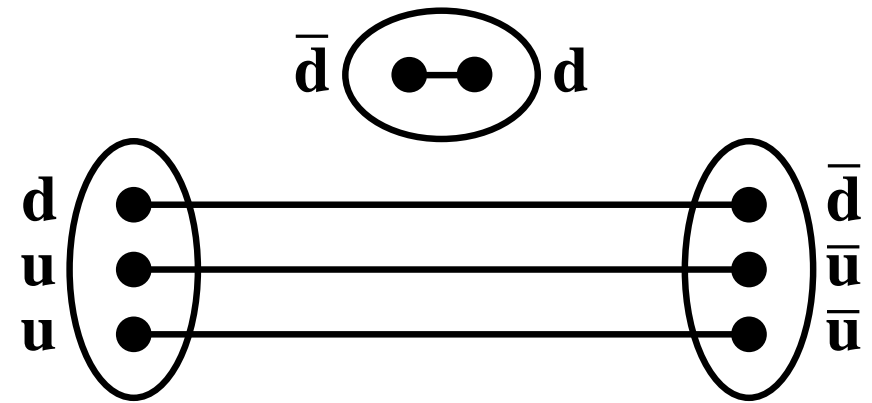
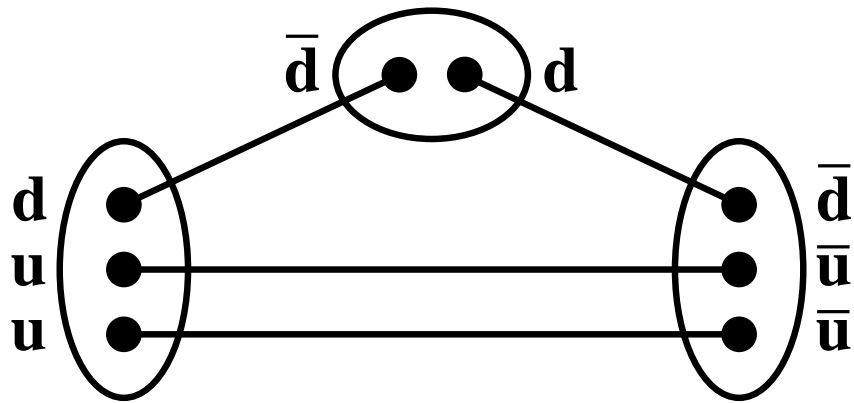
- construct the appropriate ratio of lattice correlation functions R_i

$$R_i = \sum_j B_{ij} \mathcal{O}_j^{\text{lat}}$$

- overdetermined set of observables

$$R_i = \sum_{\alpha=1}^{n+1} C_{i\alpha} F_\alpha(t) \quad \chi^2 = \sum_i \left(\frac{\sum_{\alpha=1}^{n+1} C_{i\alpha} F_\alpha(t) - R_i}{\sigma_i} \right)^2$$

Connected & Disconnected Diagrams



- connected diagrams require $18 = 3 \cdot 2 \cdot 3$ Dirac matrix inversions per gauge field, determines non-singlet matrix elements ($u - d$) for $m_u = m_d$
- disconnected diagrams require $\# \cdot (t_{\text{sink}} - t_{\text{source}}) \cdot V$ Dirac matrix inversions per gauge field, necessary for singlet matrix elements ($u + d$)
- other methods: truncated eigenmode approach, stochastic estimation, wall source technique

Our Results

I. Simulation Parameters

II. Form Factors

III. Quark Angular Momenta

IV. Transverse Quark Distributions

Simulation Parameters

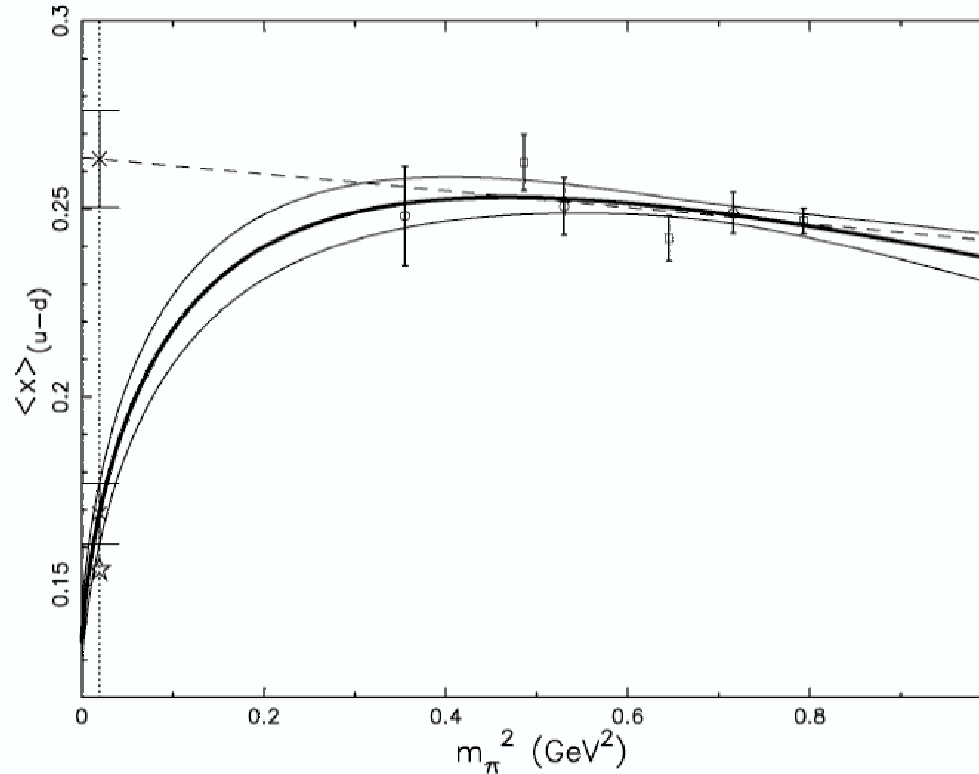
- SESAM gauge fields
- $N_F = 2$ Wilson fermions
- $a = 0.092$ fm, $L = 1.48$ fm, $16^3 \times 32$
- O(200) gluon configurations
- $M_\pi = 744, 831, 897$ MeV

Chiral Extrapolations

- leading order χ PT & heavy quark limit

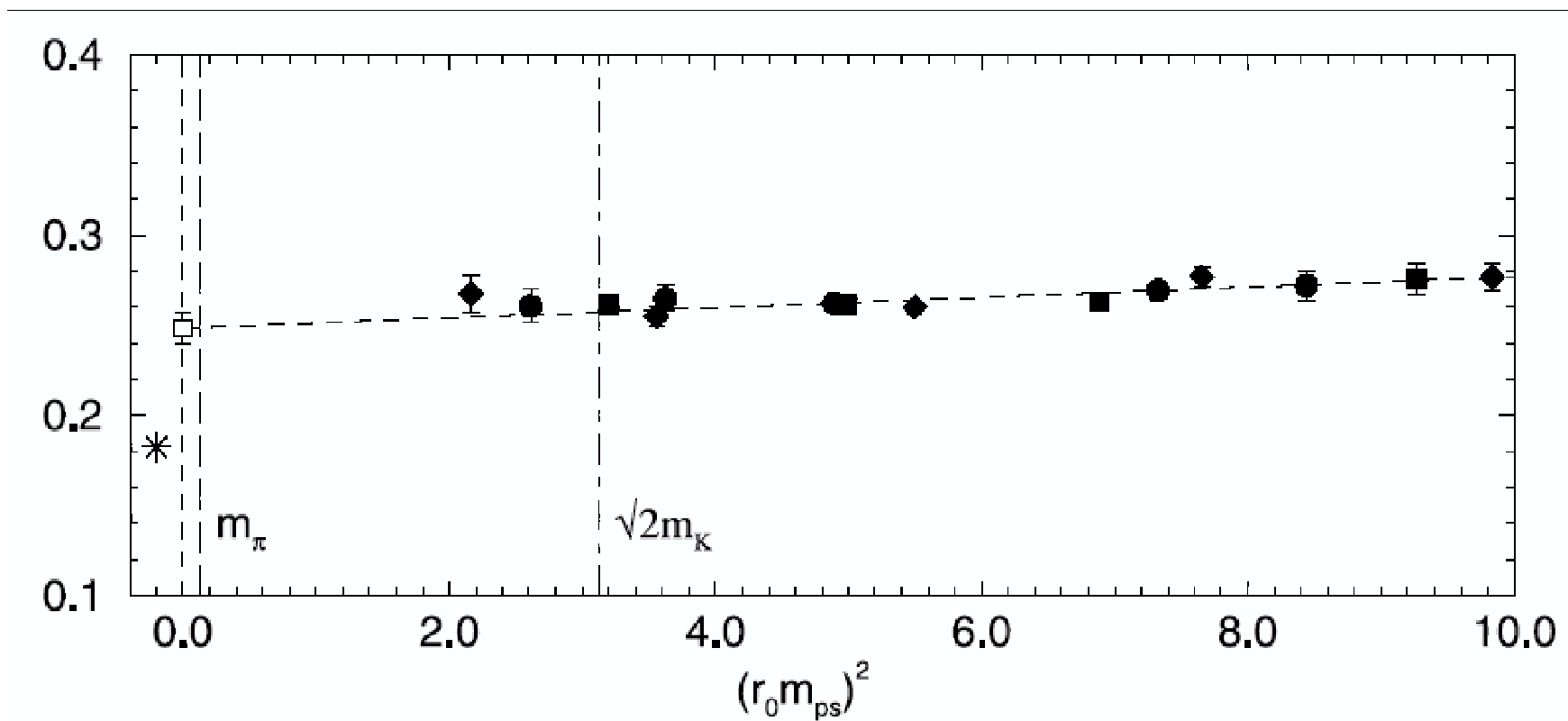
$$\langle x^n \rangle_{u-d} = a_n \left(1 - \frac{(3g_A^2 + 1)m_\pi^2}{(4\pi f_\pi)^2} \ln \left(\frac{m_\pi^2}{m_\pi^2 + \mu^2} \right) \right) + b_n m_\pi^2$$

- $\langle x \rangle$ for SESAM full QCD



Heavy Pion World

- linear m_π^2 regime
- $\langle x \rangle$ for QCDSF quenched QCD

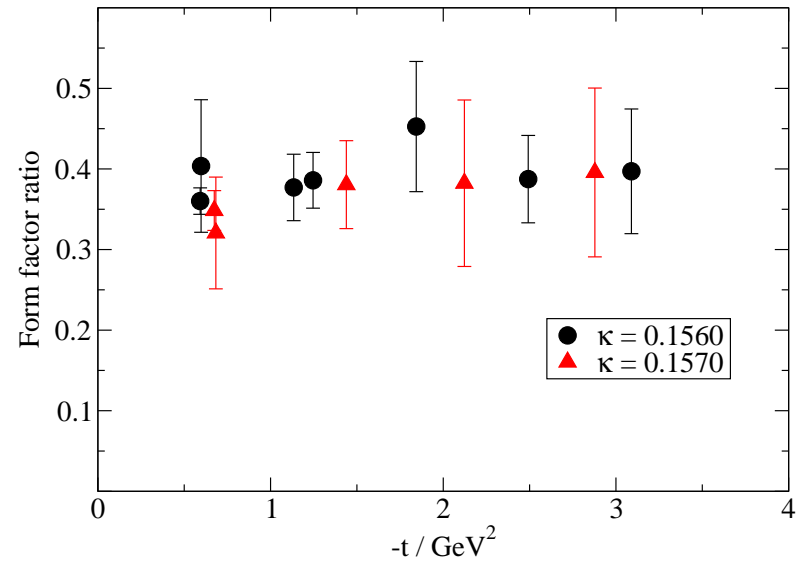
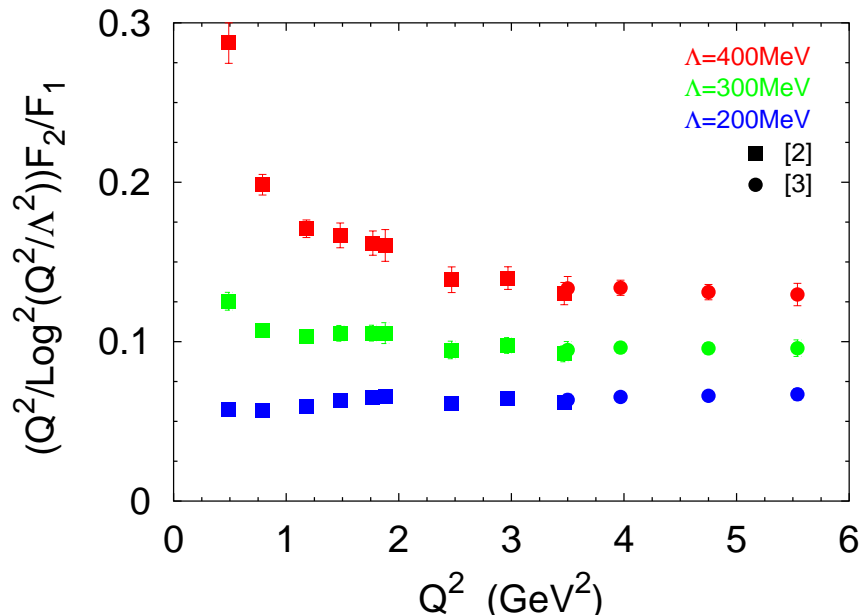


Form Factor Ratios

- quark counting rules & perturbative QCD

$$\frac{Q^2 F_2(Q^2)}{F_1(Q^2)} \sim \text{constant}$$

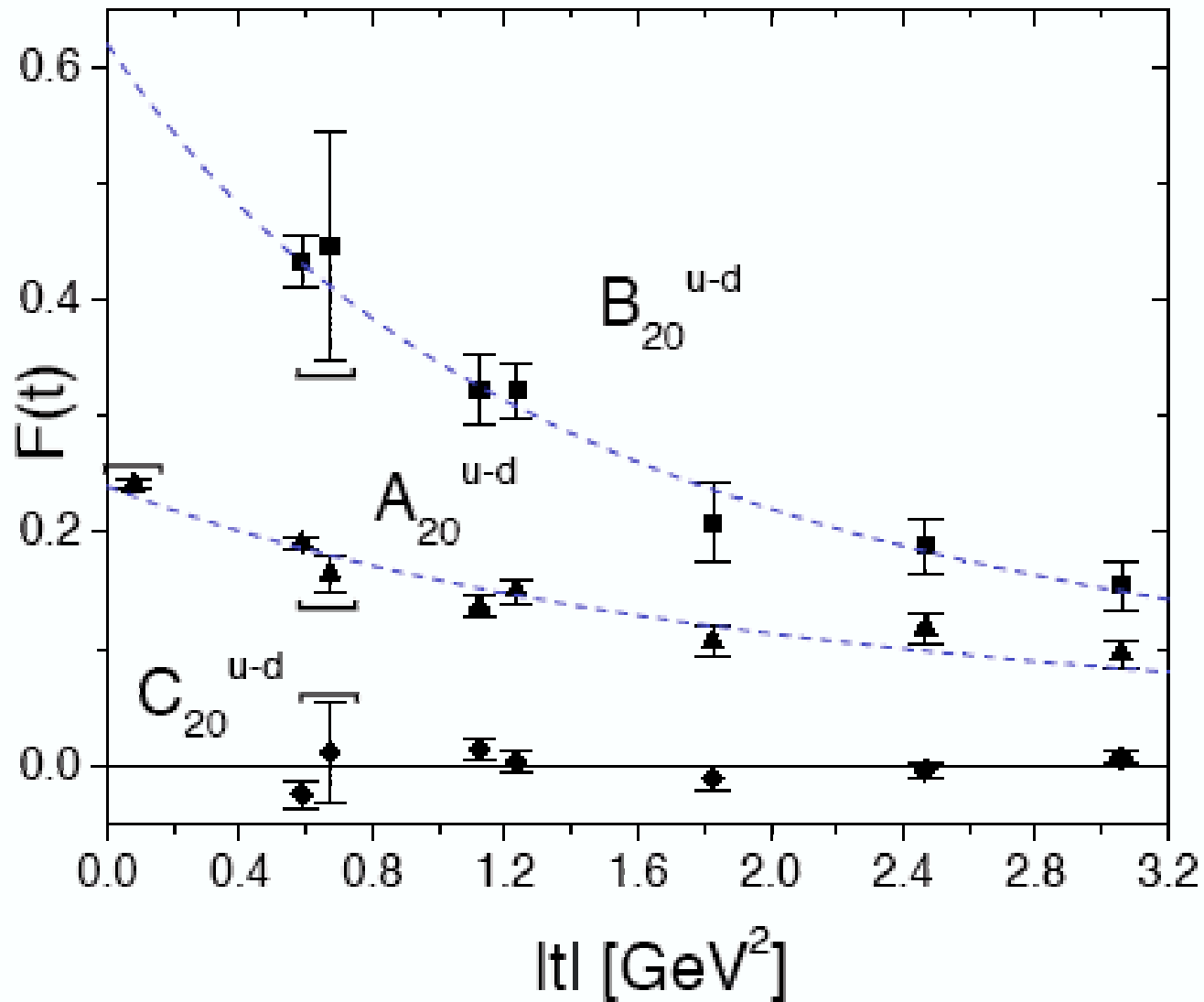
$$\frac{Q^2 F_2(Q^2)}{\log^2(Q^2/\Lambda^2) F_1(Q^2)} \sim \text{constant}$$



- note normalization difference: compare right plot with 2.79 times left plot

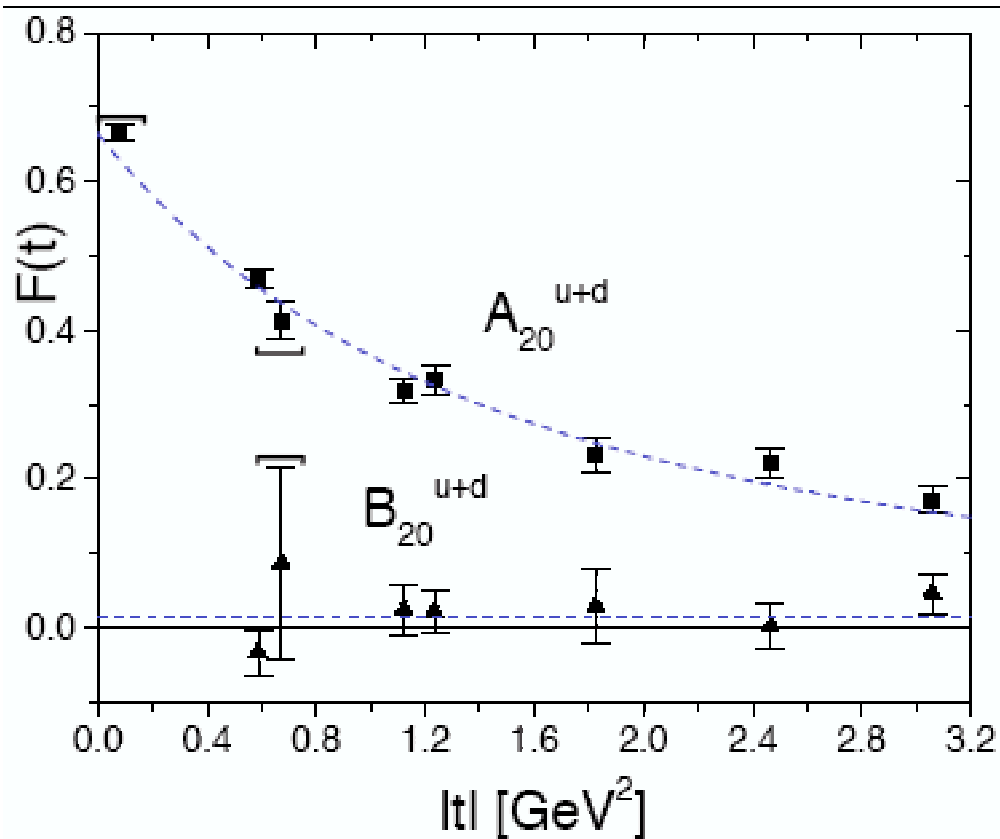
Generalized Form Factors

- $\bar{\psi}\gamma(\mu D^\nu)\psi$ has 3 GFFs: A_{20} , B_{20} , C_2



Quark Angular Momentum: $m_\pi = 897\text{MeV}$

- $\frac{1}{2}\Delta\Sigma_{u+d} = \frac{1}{2}\tilde{A}_{10}^{u+d}(0) = \frac{1}{2}(\langle 1 \rangle_{\Delta u} + \langle 1 \rangle_{\Delta d}) \sim \frac{1}{2}0.682(18)$
- $J_{u+d} = \frac{1}{2}(A_{20}^{u+d}(0) + B_{20}^{u+d}(0)) \sim \frac{1}{2}0.675(7)$
- $L_{u+d} = J_{u+d} - \frac{1}{2}\Delta\Sigma_{u+d} \sim 0 \Rightarrow J_g = \frac{1}{2}0.32$



Transverse Structure

$$H_q(x, 0, -\vec{\Delta}_\perp^2) = \int d^2 b_\perp e^{i\vec{\Delta}_\perp \cdot \vec{b}_\perp} q(x, \vec{b}_\perp)$$

$$A_{n0}^q(t) = \int_{-1}^1 dx x^{n-1} H_q(x, 0, t)$$

- at $x = 1$ a single quark carries all the momentum

$$\lim_{x \rightarrow 1} q(x, \vec{b}_\perp) \propto \delta^2(\vec{b}_\perp) \quad H_q(1, 0, t) = \text{constant}$$

- higher moments A_{n0}^q weight $x \sim 1$ more heavily

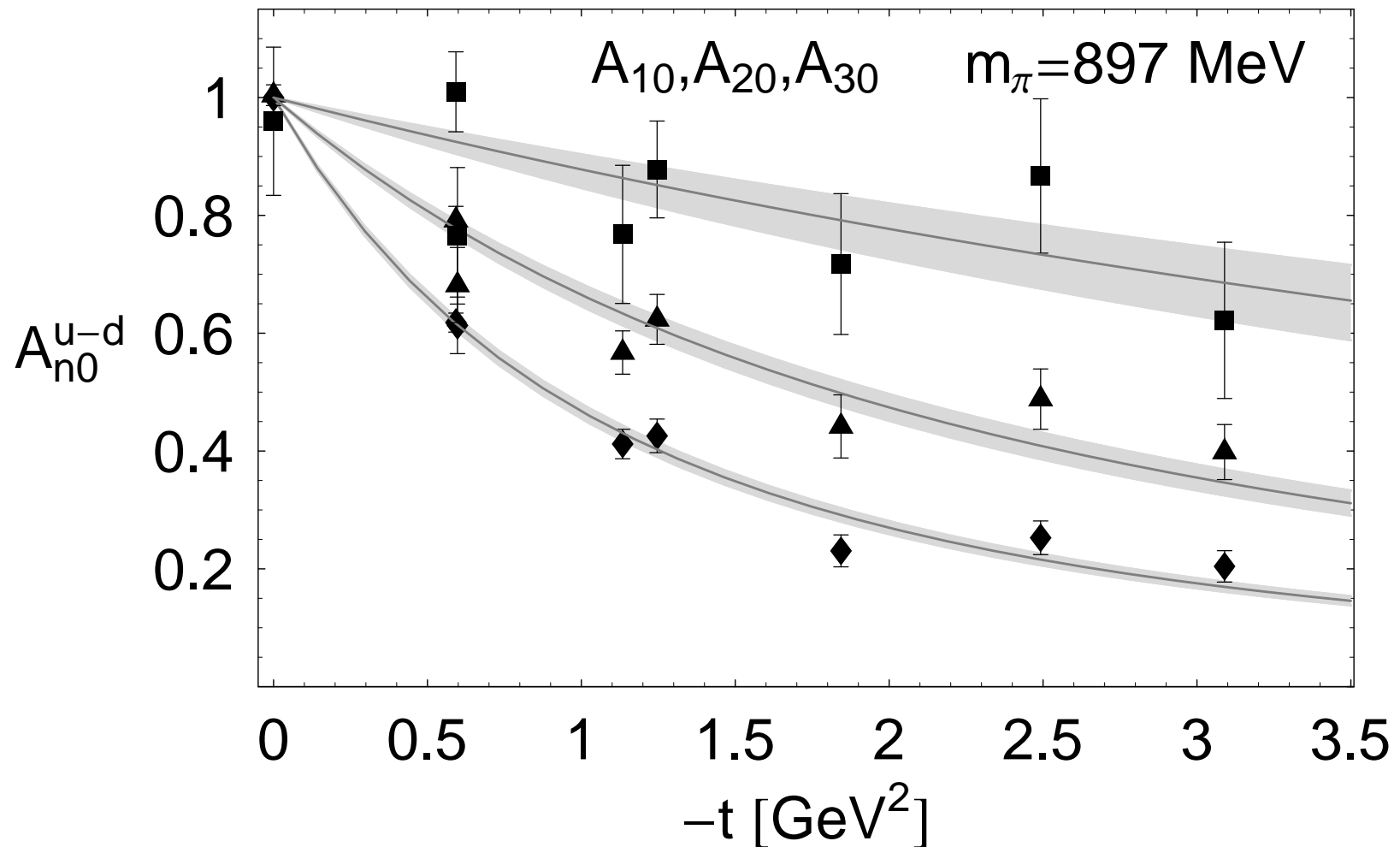
$$\lim_{n \rightarrow \infty} A_{n0}^q(t) \propto H_q(1, 0, t)$$

- slopes of A_{n0}^q should decrease as n increases

- $A_{10}, A_{30}, \tilde{A}_{20}$ measure $q - \bar{q}$ & $\tilde{A}_{10}, \tilde{A}_{30}, A_{20}$ measure $q + \bar{q}$

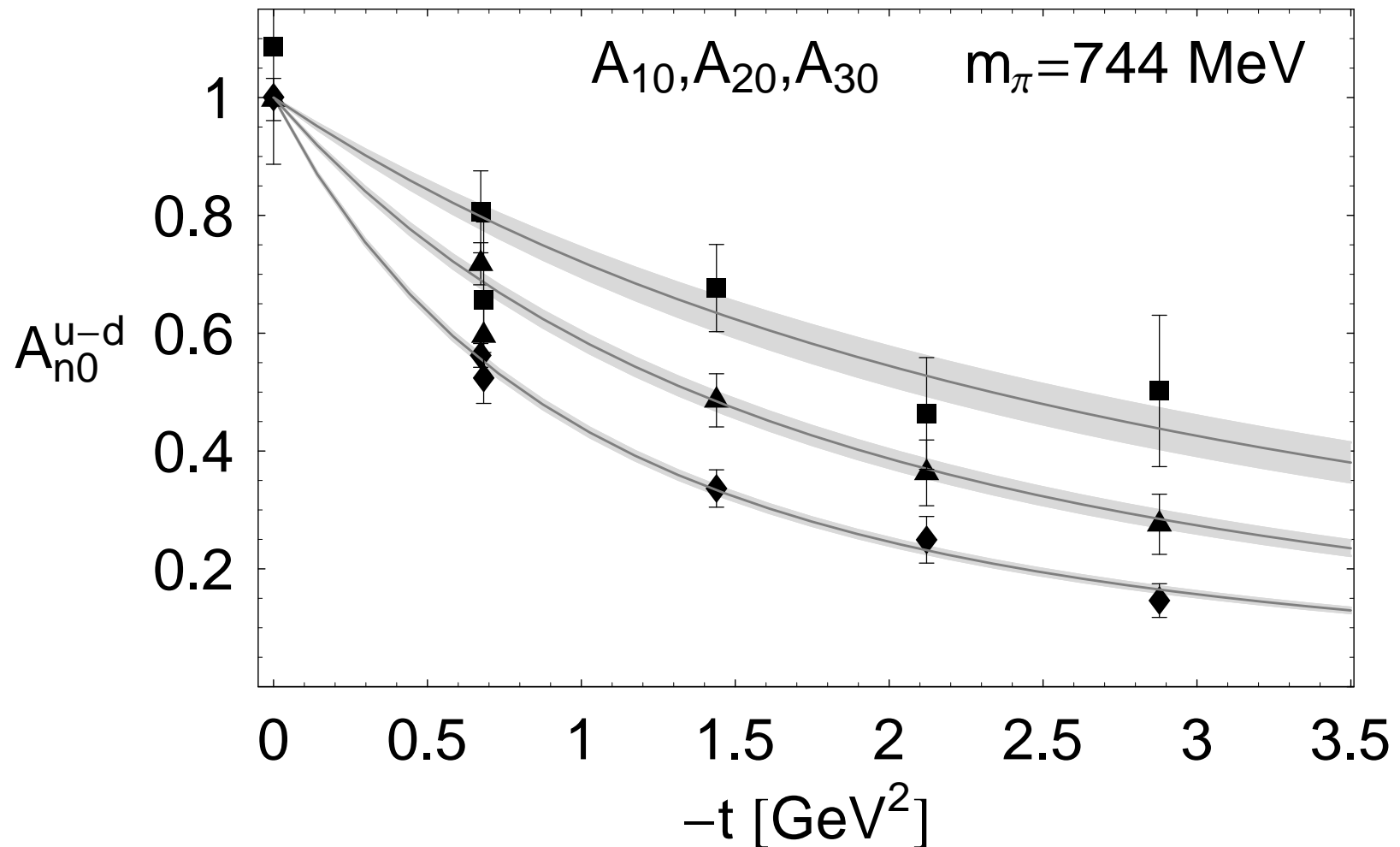
Transverse Structure: $m_\pi = 897\text{MeV}$

- slope of $A_{10}^{u-d} = -0.93 \pm 0.04 \text{ (GeV)}^{-2}$
- slope of $A_{30}^{u-d} = -0.13 \pm 0.03 \text{ (GeV)}^{-2}$ (factor of 7)



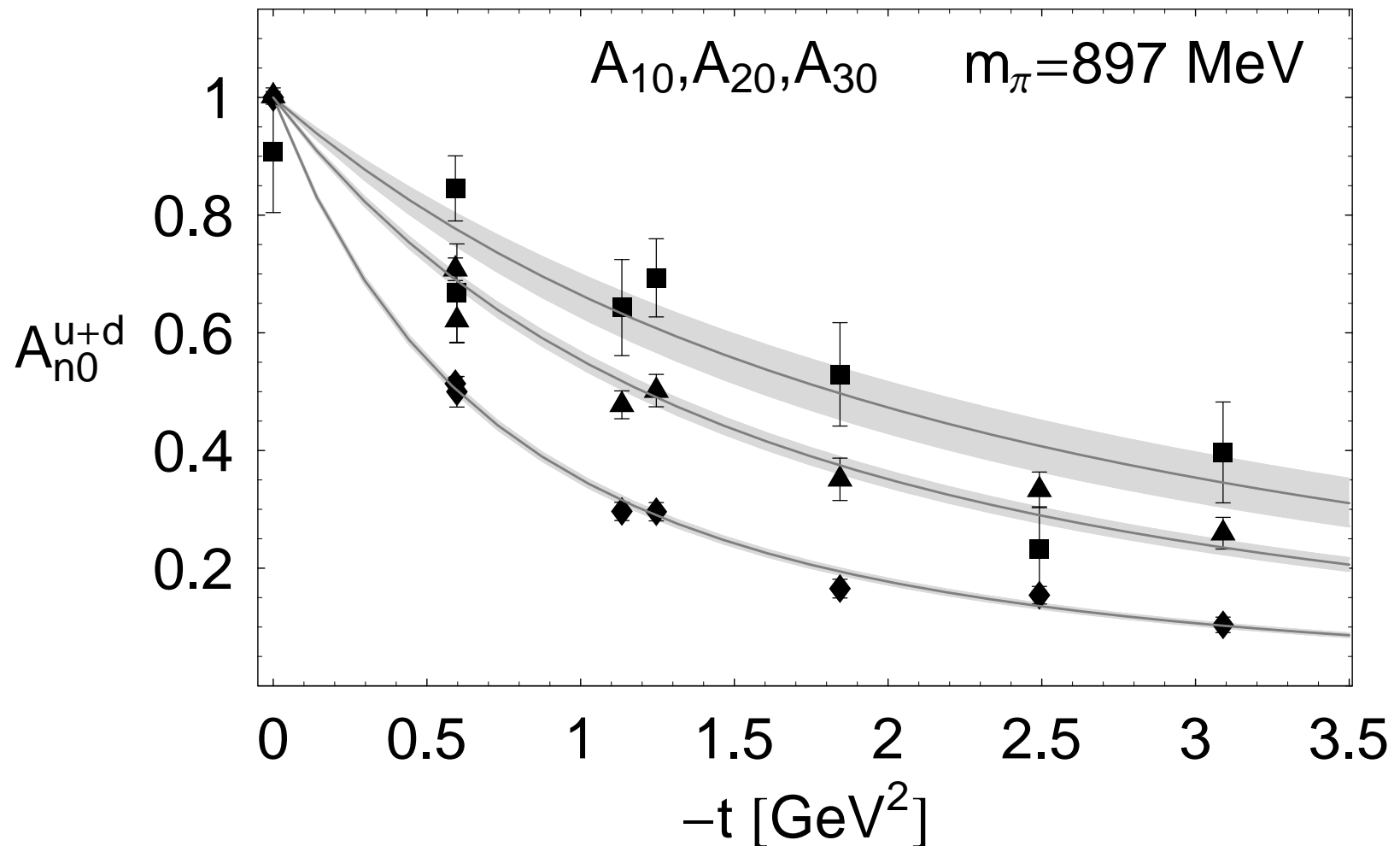
Transverse Structure: $m_\pi = 744\text{MeV}$

- slope of $A_{10}^{u-d} = -1.02 \pm 0.03 \text{ (GeV)}^{-2}$
- slope of $A_{30}^{u-d} = -0.36 \pm 0.04 \text{ (GeV)}^{-2}$ (factor of 3)



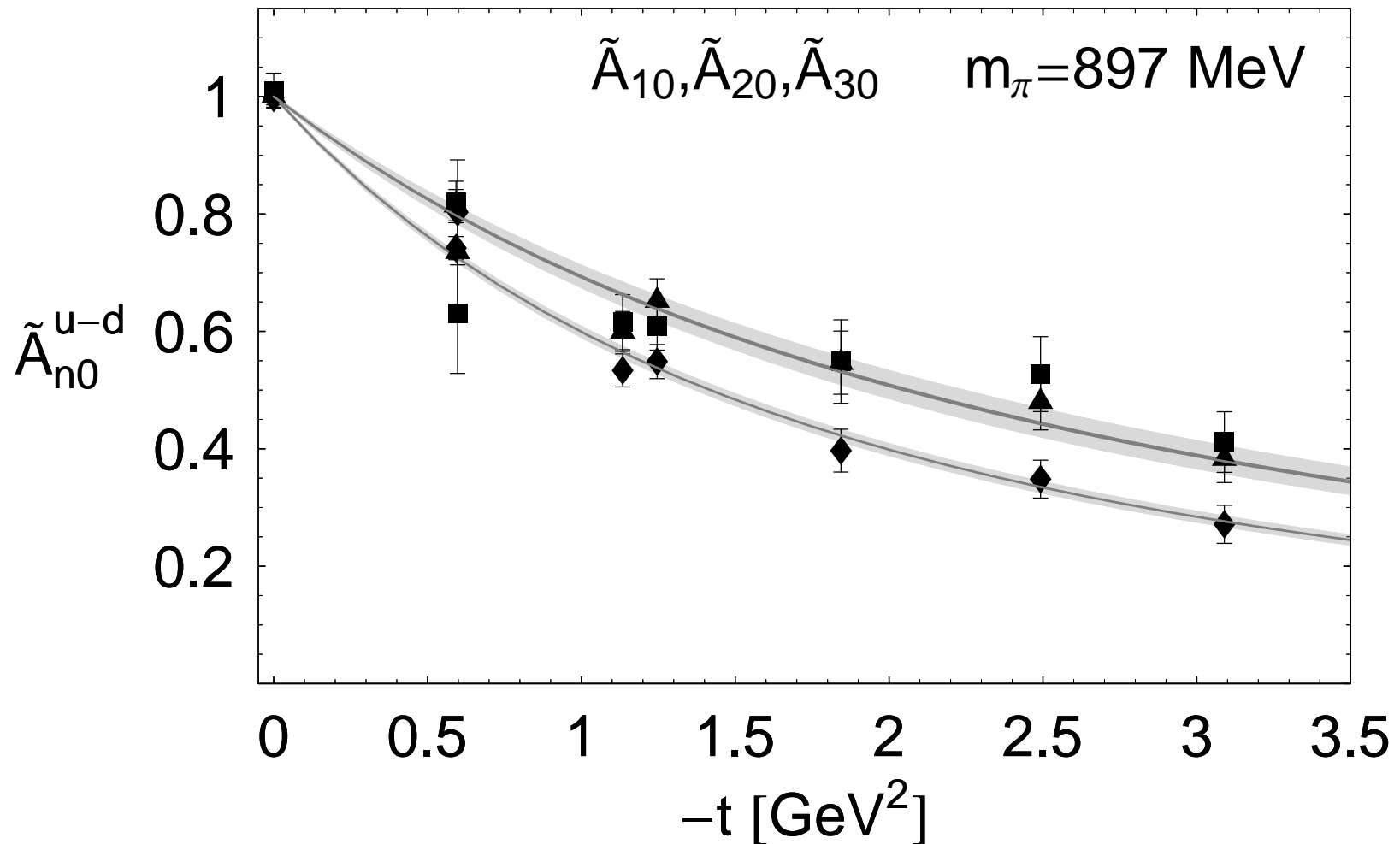
Transverse Structure: Flavor Dependence

- slope of $A_{10}^{u+d} = -1.38 \pm 0.03 \text{ (GeV)}^{-2}$
- slope of $A_{30}^{u+d} = -0.45 \pm 0.07 \text{ (GeV)}^{-2}$ (factor of 3)



Transverse Structure: Spin Dependence

- slope of $\tilde{A}_{10}^{u-d} = -0.58 \pm 0.02 \text{ (GeV)}^{-2}$
- slope of $\tilde{A}_{30}^{u-d} = -0.40 \pm 0.03 \text{ (GeV)}^{-2}$ (factor of 1.5)



Transverse Structure

- transverse rms radius

$$\langle b_{\perp}^2 \rangle_x = \frac{\int d^2 b_{\perp} b_{\perp}^2 q(x, \vec{b}_{\perp})}{\int_{-1}^1 dx \int d^2 b_{\perp} q(x, \vec{b}_{\perp})}$$

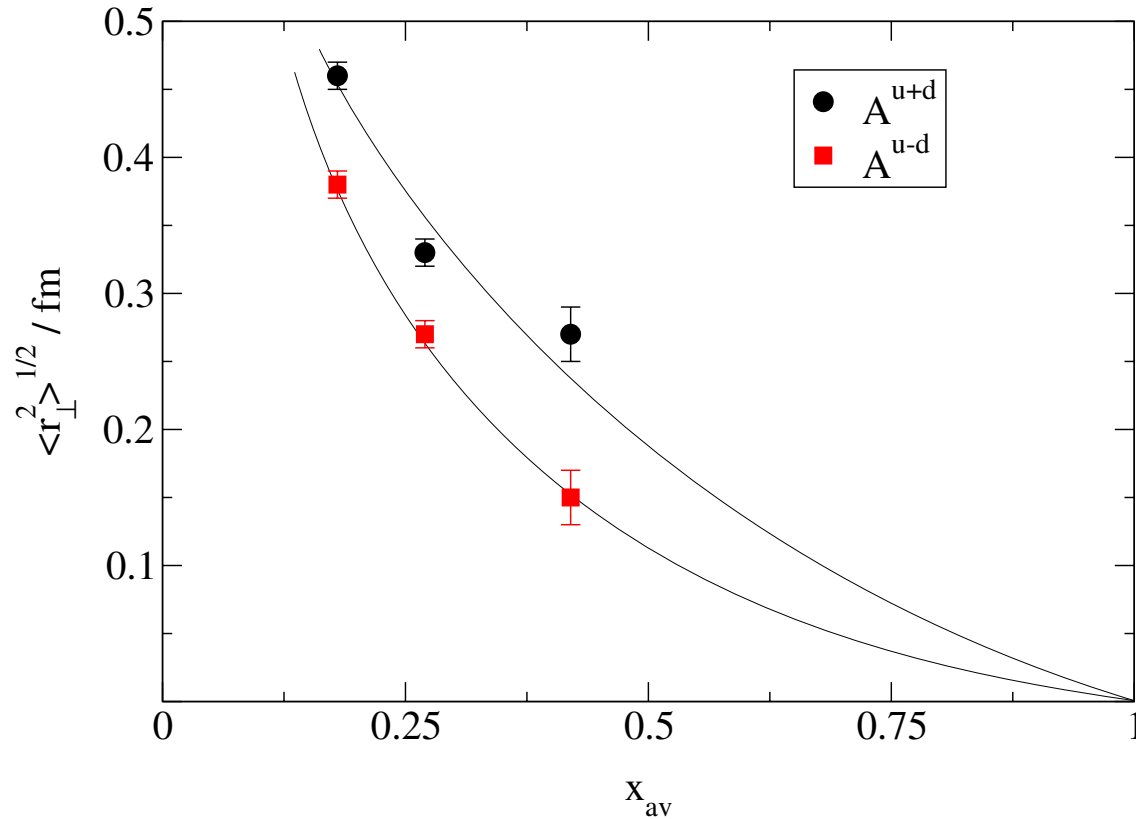
- smeared transverse rms radius

$$\frac{A'_{n0}(0)}{A_{n0}(0)} = -\frac{1}{4} \langle b_{\perp}^2 \rangle_{(n)} \quad \langle b_{\perp}^2 \rangle_{(n)} = \frac{\int_{-1}^1 dx \int d^2 b_{\perp} b_{\perp}^2 x^{n-1} q(x, \vec{b}_{\perp})}{\int_{-1}^1 dx \int d^2 b_{\perp} x^{n-1} q(x, \vec{b}_{\perp})}$$

- the average x in $\langle b_{\perp}^2 \rangle_{(n)}$

$$x_{\text{av}}^{(n)} = \frac{\int_{-1}^1 dx \int d^2 b_{\perp} x \cdot x^{n-1} q(x, \vec{b}_{\perp})}{\int_{-1}^1 dx \int d^2 b_{\perp} x^{n-1} q(x, \vec{b}_{\perp})} = \frac{\langle x^n \rangle}{\langle x^{n-1} \rangle}$$

Smeared Transverse Structure



- charge radius: $\sqrt{\langle b_{\perp}^2 \rangle_{\text{charge}}} = 0.42 \text{ fm}$ (0.72 fm from experiment), no pion cloud
- non-singlet radius: $\sqrt{\langle b_{\perp}^2 \rangle_{u-d}^{(1)}} = 0.38 \text{ fm}$ & $\sqrt{\langle b_{\perp}^2 \rangle_{u-d}^{(3)}} = 0.15 \text{ fm}$, 61% decrease
- singlet radius: $\sqrt{\langle b_{\perp}^2 \rangle_{u+d}^{(1)}} = 0.46 \text{ fm}$ & $\sqrt{\langle b_{\perp}^2 \rangle_{u+d}^{(3)}} = 0.27 \text{ fm}$, 41% decrease

Current Work: Chiral Limit

- hybrid calculation: Asqtad staggered sea quarks (MILC) & domain wall valence quarks with HYP smearing
- $a = 0.13$ fm, $L = 2.6$ fm, $20^3 \times 32$
- $M_\pi = 343, 635$ MeV
- $O(100)$ gluon configurations
- extended statistics, intermediate masses, volume dependence

Transverse Structure of Nucleon Parton Distributions

Summary

- generalized parton distribution $H_q(x, \xi \rightarrow 0, t)$ measures Fourier transform of transverse quark distribution
- building blocks method to determine all matrix elements for parton distributions, form factors, and generalized parton distributions
- overdetermined observables method to accurately measure generalized form factors upto 3 GeV^2
- observed significant dependence of slopes of generalized form factors A_{n0} on n indicating a significant variation of transverse size with x